

Left Ventricular Finite Element Model Bounded by a Systemic Circulation Model

A. I. Veress

Department of Mechanical Engineering,
Department of Bioengineering,
University of Washington,
Seattle, WA 98195

G. M. Raymond

Department of Bioengineering,
University of Washington,
Seattle, WA 98195

G. T. Gullberg

Life Science Division,
E. O. Lawrence Berkeley National Laboratory,
Berkeley, CA 94720;
Department of Radiology,
University of California San Francisco,
San Francisco, CA 94122

J. B. Bassingthwaite

Department of Bioengineering,
University of Washington,
Seattle, WA 98195

A series of models were developed in which a circulatory system model was coupled to an existing series of finite element (FE) models of the left ventricle (LV). The circulatory models were used to provide realistic boundary conditions for the LV models. This was developed for the JSim analysis package and was composed of a systemic arterial, capillary, and venous system in a closed loop with a varying elastance LV and left atria to provide the driving pressures and flows matching those of the FE model. Three coupled models were developed, a normal LV under normotensive aortic loading (116/80 mm Hg), a mild hypertension (137/89 mm Hg) model, and a moderate hypertension model (165/100 mm Hg). The initial step in the modeling analysis was that the circulation was optimized to the end-diastolic pressure and volume values of the LV model. The cardiac FE models were then optimized to the systolic pressure/volume characteristics of the steady-state JSim circulatory model solution. Comparison of the stress predictions for the three models indicated that the mild hypertensive case produced a 21% increase in the average fiber stress levels, and the moderate hypertension case had a 36% increase in average stress. The circulatory work increased by 18% and 43% over that of the control for the mild and moderate hypertensive cases, respectively. [DOI: 10.1115/1.4023697]

Keywords: hypertension, finite element, left ventricle, circulation, integrative modeling, myocardial stress and strain, numerical methods, simulation systems, pressure-flow relationships, cardiac output, ejection fraction, cardiac physiome

Introduction

Finite element models have been applied to study the effects of ischemia [1,2] and infarction [3–5] on the left ventricle as well as used

to evaluate the effectiveness of cardiac interventions such as the repair of infarction induced aneurysms [6–9]. One of the limitations of these types of FE models is that they have not been connected to a model of the circulatory system so that the reflections of the pressure waves back to the heart from the arterial system and their influence on the contractile process are not represented. Instead, a priori boundary conditions are assigned to the models based on typical vascular pressure loading to predict the cardiac strain/stress.

In order to overcome this problem, Kerckhoffs et al. [10] embedded a full zero-dimensional (0D) circulatory system into the Continuity simulation package¹, thus providing the appropriate boundary conditions to a 3D FE biventricular mechanical model [11,12]. The tight integration of the circulation with the solid model allows for direct exchange of LV pressure/volume information between the two parts of the simulation package, but this system is computationally expensive.

The primary goal of the following work was to create a framework that allows for the communication of pressure and volume values back and forth between two distinct and dissimilar modeling systems, thus linking a 0D circulatory model to a 3D finite-element LV mechanical model. The circulatory model was run under the JSim [13] analysis package² while the LV models were developed for and analyzed using the general purpose, nonlinear, large deformation FE package NIKE3D [14]. Due to limitations in the communication pathway between the circulatory and FE models, this type of coupling can be considered “weak” or “loosely” coupled rather than the direct coupling illustrated by the work of Kerckhoffs et al. [10].

Materials and Methods

The coupled JSim/FE models were composed of three parts, each of which will be described in detail below. The first component was a circulatory system run using JSim. The second component was the FE LV mechanical model that runs under NIKE3D. The third component, the JSim/FE interface, controls the communication of information between these two modeling systems as well as providing the means to optimize the FE LV active contraction parameters of the FE model so that it reproduces the pressure/volume characteristics of the JSim simulation.

JSim Circulatory Model. The JSim model of the systemic circulation contains the left atria, left ventricle, the aorta, and the rest of the systemic circulation (arteries, capillaries, and venous return) (Fig. 1) and is a reduced form of the Neal and Bassingthwaite [15,16] model. The systemic circulations were modeled using three lumped Windkessel compartments in series, one compartment for the aorta, another for the arteries and capillary blood, and another for the venous blood. The right heart and the pulmonary systems were lumped into the venous return. The left atria and left ventricle are represented using time-varying elastance models. All the equations are listed in Appendix A.

Left Ventricle Mechanical Model. A complete description of the LV model can be found in Veress et al. [1,5] (Fig. 2). Briefly, the passive myocardium was represented as transversely isotropic [17] with a time varying elastance active contraction component [18,19].

The total Cauchy stress in the fiber direction \mathbf{a} is given as $T = \mathbf{T}(\mathbf{a} \otimes \mathbf{a})$ and is the sum of the active stress $T^{(a)}$ and the passive stress tensor $T^{(p)}$ component due to the transversely isotropic material model in the fiber direction as follows:

$$T = T^{(p)} + T^{(a)} \quad (1)$$

The active fiber stress $T^{(a)}$ is defined as

$$T^{(a)} = T_{\max} \frac{Ca_0^2}{Ca_0^2 + ECa_{50}^2} C_t \quad (2)$$

Contributed by the Bioengineering Division of ASME for publication in the JOURNAL OF BIOMECHANICAL ENGINEERING. Manuscript received June 19, 2012; final manuscript received January 3, 2013; accepted manuscript posted February 19, 2013; published online April 24, 2013. Assoc. Editor: Jeffrey W. Holmes.

¹For more information, see www.continuity.ucsd.edu.

²For more information, see www.physiome.org.

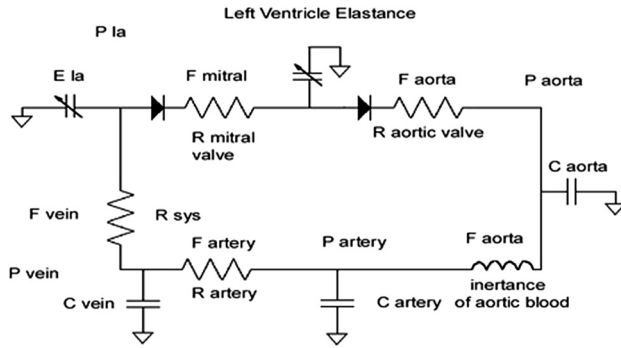


Fig. 1 Schematic of the systemic JSim model of FE heart model and model of circulatory system. The labels are P for the pressure values, F for the flow, R for the resistance, C for the compliance, and L for the inertance at the given locations shown above. The left atria and ventricle are represented as a time varying elastance units.

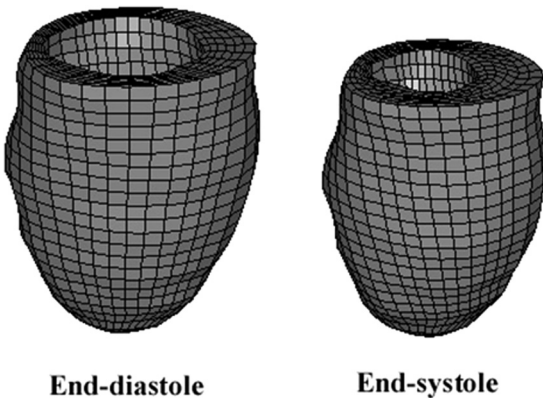


Fig. 2 The left ventricle FE model in the end-diastolic (left) and end-systolic (right) configurations

where $T_{\max} = 135.7$ KPa is the isometric tension under maximal activation at the peak intracellular calcium concentration of $Ca_0 = 4.35 \mu\text{M}$ [19]. C_t governs the shape of the activation curve [19], which is only defined during contraction. The product of the constant T_{\max} and C_t defines the primary boundary condition in the mechanical model input file and was zero during diastole and controls active contraction during systole. The length dependent calcium sensitivity ECa_{50} is governed by the following equation:

$$ECa_{50} = \frac{(Ca_0)_{\max}}{\sqrt{\exp[B(l - l_0) - 1]}} \quad (3)$$

where $(Ca_0)_{\max} = 4.35 \mu\text{M}$ is the peak intracellular calcium concentration, $B = 4.75 \mu\text{m}^{-1}$ governs the shape of the peak isometric tension-sarcomere length relation, $l_0 = 1.58 \mu\text{m}$ is the sarcomere length at which no active tension develops, and l is the sarcomere length, which is the product of the fiber stretch ratio λ , and the unloaded length $l_r = 2.04 \mu\text{m}$ [18,19].

Coupled Analysis. The coupled analysis begins with the analysis of the baseline FE LV model in order to provide the JSim circulatory model with diastolic pressure/volume characteristics based on literature values [19,20]. The end-diastolic pressure/volumes were passed to JSim where a SENSOP optimization routine [21,22] was utilized to tailor the circulatory model so that the diastolic pressure and volume characteristics of the FE model were reproduced in the circulatory model. This was accomplished through the optimization of the systemic resistance (R_{ar}) and

capacitance (C_{ar}) values and the maximum elastance of the left ventricle ($E_{\max lv}$).

Upon completion of the diastolic optimization, the circulatory model was run until equilibrium was achieved (five cardiac cycles). JSim then initiated the interface program by issuing a command to the Linux operating system. The interface program provided the communication pathway between the JSim circulatory model and the ventricular FE mechanical model.

JSim Interface Program. The interface program was composed of two parts. The first part reads in pressure and volume values at four points during the ejection phase of systole exported from JSim as a text file. These were 408, 413, 417, and 420 ms from the beginning of diastole (reference configuration $t = 0$ with an 800 ms cardiac cycle time). Peak systolic pressure was achieved at 417 ms. These time points represent the ejection phase of systole when the aortic valve is open. The NIKE3D LV model file was read by the interface program, and the JSim-derived LV pressure values were substituted for those of the original Nike model. The interface program initiated the FE analysis of the model, which was the starting point for the subsequent systolic optimizations. For this initial run, the FE analysis of the entire cardiac cycle was completed with the analysis starting with the model at reference, beginning diastolic configuration, proceeding through passive filling followed by contraction, and finally relaxation from the contracted state.

The active contraction stress values of the LV model were then optimized until the difference in the NIKE3D volumes (Appendix B) and the JSim volumes reached a user defined tolerance. This was accomplished using a secant [24] type iteration scheme (Eq. (4)), which uses an estimate of the derivative based upon the current and previous iterations (Eq. (5)). The derivative of the active contraction stress/error function was used to determine the next active contractile stress values via the setting of C_t as given below:

$$C_{t_{n+1}} = C_{t_n} - \alpha \frac{f_n}{f'_n} \quad (4)$$

where n is the current iteration, $n - 1$ is the previous iteration, and $n + 1$ is the next iteration. α is a damping factor having a value of 0.5. The damping factor was necessary due to the highly nonlinear nature of the stress/volume relationship. The derivative f' was defined as:

$$f' = \frac{df}{dC_t} = \frac{(f_n - f_{n-1})}{(C_{t_n} - C_{t_{n-1}})} \quad (5)$$

with f being the error in volumes

$$f = \text{Vol}_{\text{JSim}} - \text{Vol}_{\text{Nike}} \quad (6)$$

The iteration scheme ran until the user defined tolerance was reached, $|f| \leq \text{tol}$ (1.5 ml). Then the analysis for this time point was completed, and the analysis would proceed to the next time point. The optimization process is shown schematically in Fig. 3. In order to save computational time, the FE analysis used for each optimization iteration was completed up to and including the time point being optimized and then was subsequently terminated.

Application: Normal and Hypertensive Hearts. Three cases were developed and analyzed with the first case being a normal LV model coupled to the circulation model that represented normotensive loading (116/80 mm Hg) measured at the aorta. Two pathologic cases were modeled with the first being mild hypertension (137/89 mm Hg) and the second being moderate hypertension (160/100 mm Hg). The hypertension circulatory models were created by systematically increasing the peripheral resistance until the hypertension values were achieved without an increase in the ejection fraction. The geometries of all of the FE models were

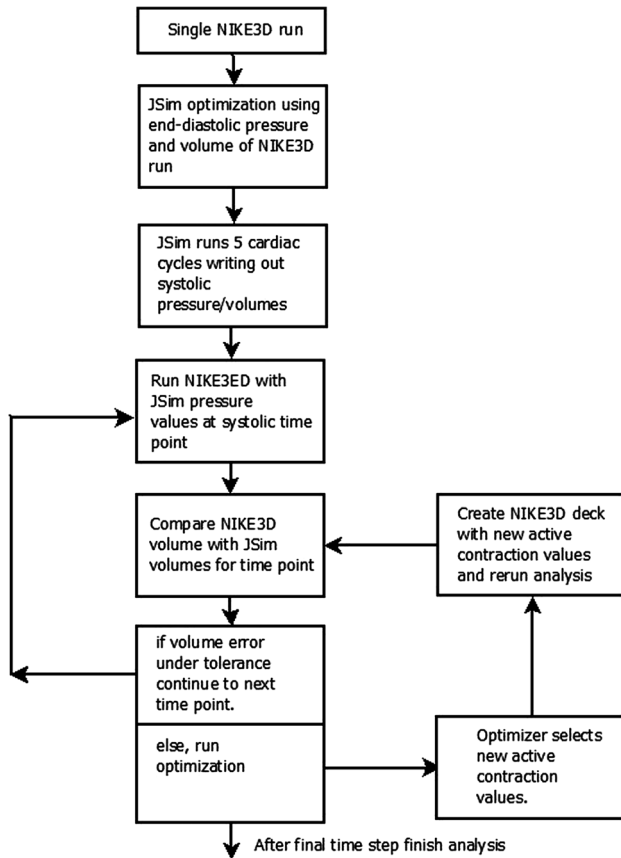


Fig. 3 Schematic of the coupled system analysis protocol. The initial step is the optimization of the circulation to the end-diastolic pressure and volume values produced by an initial run of the FE model. JSim was then run until equilibrium was achieved in the model. This was followed by optimization of the FE model to reproduce the JSim pressure and volume values at each of the four time points. Once the correct values were achieved for a given time point, the process was repeated for the next time point until all of the time points had been optimized.

identical, thus representing cases of hypertension without subsequent remodeling. The starting parameters for the normotensive systolic optimizations were based upon a previous LV model [1]. Additionally, the hypertension cases used the optimized normal FE model as the starting point for the systolic optimizations. The entire cardiac cycle was analyzed following the optimization of the final systolic time point.

FE Model Data Analysis. Upon completion of the analysis of the three cases, the average fiber stresses predicted by each of the FE models were compared. The circulatory pressure and volume characteristics were used to estimate the circulatory work.

Results

The diastolic optimizations within JSim were completed in 1 min for 150 iterations using the SENSOP optimizer run on a four core 3.2 GHz Linux computational server. The optimized diastolic LV pressure value fell within 1.0 mm Hg of the NIKE3D target value, and the end-diastolic LV volume came within 1.0 ml of the target value for all cases.

The systolic optimizations run within the interface program (Figs. 4(a) and 4(b)) required four NIKE3D iterations to ensure proper LV volume output (Fig. 5). The total analysis time was approximately 4 h. The curves labeled “starting values” in Fig. 5 are the NIKE3D volume values on the initial run following the

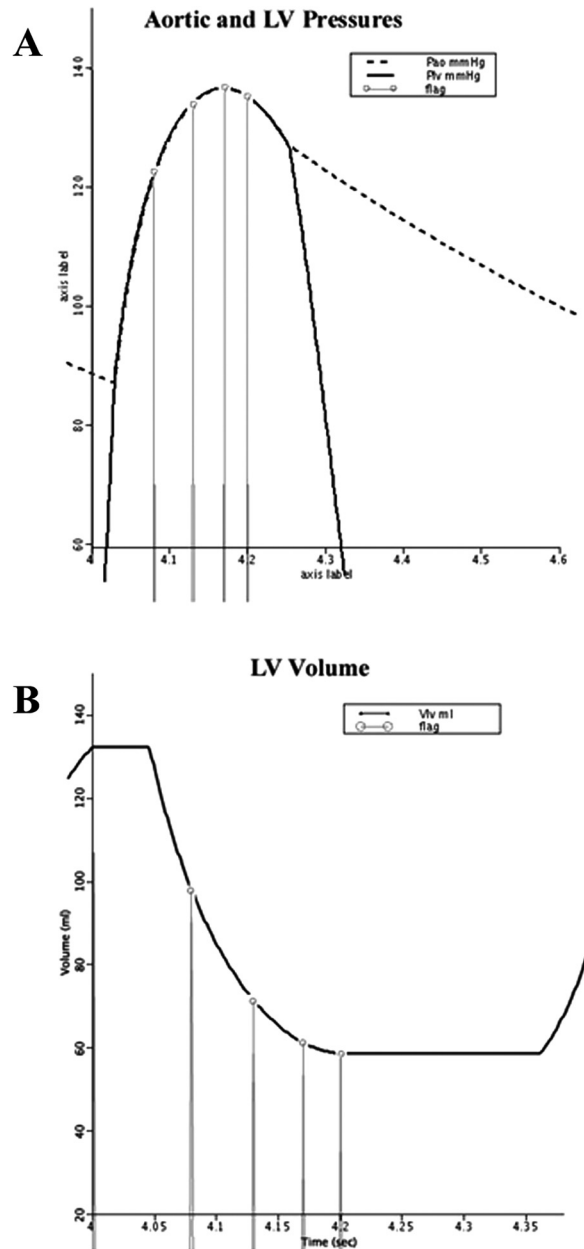


Fig. 4 (a) Aortic pressure curves (dashed black) and the left ventricular pressure curve (solid black) defined in the JSim circulatory system are given. (b) The JSim derived LV volume curve (black) used in the mild hypertensive systolic optimizations. The vertical gray lines indicate the four systolic time points for both graphs.

substitution of the JSim systolic pressure values into the LV model.

The circulatory model was able to produce realistic hemodynamic values (Table 1). The cardiac output (stroke volume) increased in the mild and moderate hypertension cases compared with the normal model. The hypertension cases showed unchanged ejection fraction values from that of the normal case.

The FE analysis prediction for the average LV fiber stress was 17.9 KPa for the normotensive case. The mild hypertensive case had an average fiber stress of 21.6 KPa, and the moderate hypertensive case had a value of 24.3 KPa (Fig. 6). These represented increases of 21% and 36% in end-systolic fiber stress.

The circulatory work indicated that the increase in peripheral resistance substantially increased the work of the heart. The circulatory work for the baseline normal case was 0.857 J, 1.015 J for mild

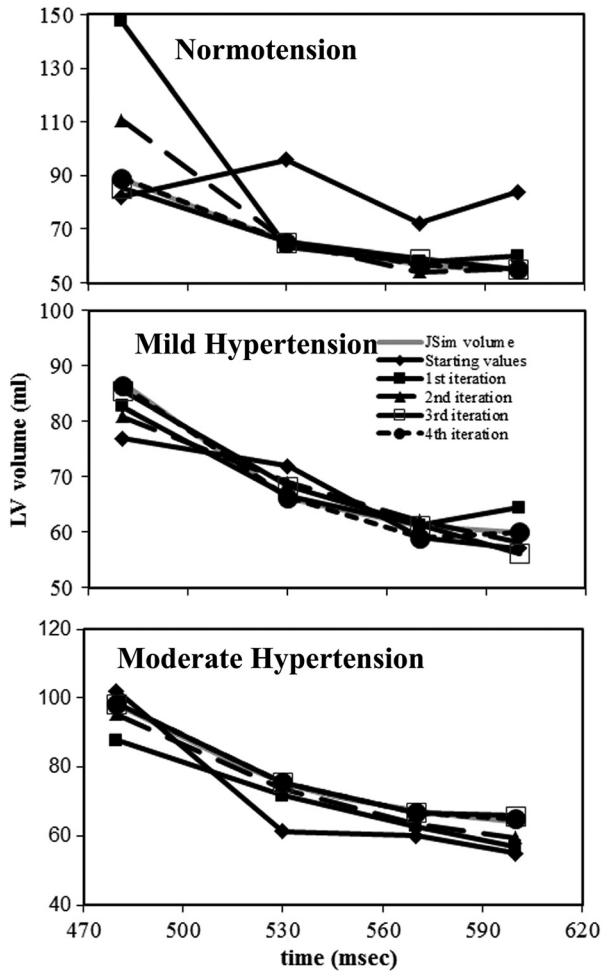


Fig. 5 Optimization to the JSim systolic volume values (gray) was achieved after four iterations all of the time points in each of the cases: normotensive (top), mild hypertension (middle), and moderate hypertension (bottom)

Table 1 Circulatory hemodynamic data

	Normal	Mild Hypertension	Moderate Hypertension
EDV	128	129	131
ESV	60	60	60
SV	69	70	71
EF	53%	54%	54%

Note: EDV = end-diastolic volume, ml; ESV = end-systolic volume, ml; SV = stroke volume, ml; EF = ejection fraction = (EVD - ESV)/EVD, dimensionless.

hypertension, and 1.223J for the moderate hypertension case. These represent 18% and 43% increases in workload, respectively.

Discussion

The use of the 0D JSim model to define the boundary conditions for the LV models resulted in a dual success, namely the development and parameterization of an FE model with constrained time-dependent physiological outflow impedance and a 0D equivalent circulatory model defining systemic arterial pressures and flows. The system in its present form is capable of modeling and having the FE LV model respond to changes in the circulatory system through altered loading of the FE model.

The analysis of the normotensive and the hypertensive cases indicate that even mild hypertension can cause a marked increase in total LV wall stress as demonstrated by the fiber stress results. The circulatory work results were consistent with these findings indicating that relatively mild increases in afterload resulted in substantially increased circulatory work values.

The optimization routines utilized in this study proved to be efficient. The SENSOP method used in this study was robust and converged quickly for the diastolic optimization of the circulatory system. The systolic optimization (secant method) showed reasonable convergence characteristics provided the starting pressure values in the FE model were within 5 mm Hg of the JSim-defined pressures. Outside this range at the end-systolic time point, the optimization had difficulty converging as the iteration solutions tended to oscillate between positive and negative errors or simply did not converge.

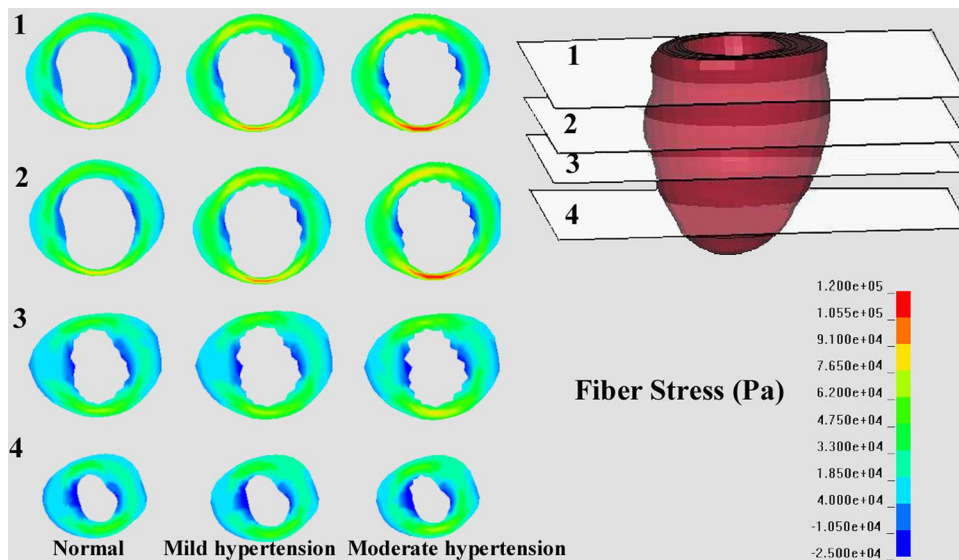


Fig. 6 Hypertension increases the fiber stress as seen in these ventricular short axis slices. These are fiber strain distributions for normal, mild, and moderate hypertension (left). The location of the slices is shown on the right.

The presented work is similar in scope with the work of Wenk et al. [24] in that a weak coupling was sought between a circulatory model and a FE based model. Wenk et al. initially tune the FE models to pressure/volume relationships found in their animal models. The models were then used to generate a family of pressure/volume curves through the definition of end-systolic pressure/volume and the end-diastolic pressure/volume relationships. These functions are passed to the circulatory model in order to tune the resistance and capacitance components. The strength of the Wenk model was that the circulatory system was tuned using a more complete relationship rather than the end-diastolic volumes and pressures as was done in our methodology. In systole, we simply let the circulatory system define the entire systolic pressure/volume relationship and then matched the FE model volumes using the pressures defined by the circulatory system. The use of discrete points to characterize the systolic contractile phase allows for optimization of experimental systolic pressure/volume data directly rather than fitting to a pressure/volume relationship.

Limitations. The primary limitation of the current implementation of this type of coupled modeling is that the transfer of information at the diastolic and four systolic time points is unidirectional instead of being bidirectional at all times. The communication necessary for heart failure and ischemia/infarction needs to be bidirectional at both diastole and systole so that the deficiencies in LV function will alter the response of the circulatory system.

Another drawback was that changes cannot be made to the circulatory parameters within a single cardiac cycle for either analysis system due to limitations inherent to both JSim and NIKE3D. The changing of parameters during the runs within JSim causes numerical instabilities that greatly alter the pressure/volume curves leading to erroneous results. While NIKE3D does have a mechanism by which the run may be interrupted and restarted, the boundary conditions cannot be changed for the continuation of the simulation.

The pressure wave forms produced by the circulatory system model tended to be overly simple. For example, the dicrotic notch does not appear in the aortic pressure waveform (Fig. 4). However, overall the waveforms do capture the relevant features of the LV pressure/volume relationship.

This work demonstrates a methodology used to couple two completely separate and dissimilar simulation packages, providing results without changing the underlying source code of either system. The system contains relatively generic components such that the interface program could be modified and applied to other dissimilar systems. With continued development, the system will be able to be used to model the boundary conditions for models that are used to define circulatory based pathologies.

Acknowledgment

We would like to acknowledge these sources of funding: NIH Grant Nos. R01-EB08407 for the JSim development, T15-HL088516 for the model archiving at www.physiome.org, and R03 EB008450, R01 EB07219, and R01 EB000121, and the Director, Office of Science, Office of Biological and Environmental Research, Biological Systems Science Division of the US Department of Energy under Contract No. DE-AC02-05CH11231 for FE model development.

Appendix A: Equations Defining the JSim Model

The equations used to describe the function of the JSim 0D circulatory system are given below.

Pressure

Pressure = elastance (volume minus resting volume) (in mm Hg)

$$P_{la} = E_{la}(V_{la} - \text{rest}V_{la}) \quad (A1)$$

$$P_{lv} = E_{lv}(V_{lv} - \text{rest}V_{lv}) \quad (A2)$$

$$P_{ao} = \frac{V_{ao} - \text{rest}V_{ao}}{C_{ao}} \quad (A3)$$

$$P_{ar} = \frac{V_{ar} - \text{rest}V_{ar}}{C_{ar}} \quad (A4)$$

$$P_{vein} = \frac{V_{vein} - \text{rest}V_{vein}}{C_{vein}} \quad (A5)$$

Flow

Flow = pressure drop/resistance (in l/min)

Δ Flow equals pressure drop/inertance

$$F_{mit} = \text{if } (P_{la} > P_{lv}) \text{ then } \frac{P_{la} - P_{lv}}{R_{mitvalve}} \text{ else } 0 \quad (A6)$$

$$F_{aov} = \text{if } (P_{lv} > P_{ao}) \text{ then } \frac{P_{lv} - P_{ao}}{R_{aorvalve}} \text{ else } 0 \quad (A7)$$

$$\frac{dF_{ao}}{dt} = \frac{P_{ao} - P_{ar}}{L_{ao}} \quad (A8)$$

$$F_{ar} = \frac{P_{ar} - P_{vein}}{R_{ar}} \quad (A9)$$

$$F_{vein} = \frac{P_{vein} - P_{la}}{R_{vein}} \quad (A10)$$

Parameter Values for Normotensive Case

E_{maxla} = 2.07 mm Hg/ml, maximum left atrium elastance
 E_{minla} = 0.15 mm Hg/ml, minimum left atrium elastance
 E_{maxlv} = 5.01 mm Hg/ml, maximum left ventricle elastance
 E_{minlv} = 0.16 mm Hg/ml, minimum left ventricle elastance
 C_{ao} = 0.14 ml/mm Hg, compliance or capacitance of aorta
 C_{ar} = 1.32 ml/mm Hg, compliance of systemic arteries
 C_{vein} = 42.1 ml/mm Hg, compliance of systemic veins
 $\text{rest}V_{lad}$ = 43.9 ml, end-diastolic rest volume left atrium
 $\text{rest}V_{las}$ = 54.4 ml, end-systolic rest volume right atrium
 $\text{rest}V_{lvd}$ = 56.2 ml, end-diastolic rest volume left ventricle
 $\text{rest}V_{lvs}$ = 37.6 ml, end-systolic rest volume right ventricle
 $\text{rest}V_{ao}$ = 22.8 ml, rest volume of aorta
 $\text{rest}V_{ar}$ = 184.1 ml, rest volume of systemic arteries
 $\text{rest}V_{vein}$ = 593.3 ml, rest volume of systemic veins
 $R_{mitvalve}$ = 0.003 mm Hg*s/ml, resistance of mitral valve
 $R_{aorvalve}$ = 0.001 mm Hg*s/ml, resistance of aortic valve
 L_{ao} = 1.e-8 mm Hg*s²/ml, inertance of aorta
 R_{ar} = 0.78 mm Hg*sec/ml, resistance of systemic arteries
 R_{vein} = 0.26 mm Hg*sec/ml, resistance of systemic veins
 HeartRate = 1.25 Hz, heart rate (75 beats/min)
 $\text{P}R_{int}$ = 0.16 s, P-R interval
 yl_{offset} = 0.5 s, offset for left atrium activation
 $yl_{voffset}$ = 0.0 s, offset for left ventricle activation

Variable Definitions

$E_{la}(t)$ mm Hg/ml, elastance of left atrium
 $E_{lv}(t)$ mm Hg/ml, elastance of left ventricle
 $yl_{a}(t)$ dimensionless, activation function for atrial elastance
 $yl_{v}(t)$ dimensionless, activation function for ventricle elastance
 $\text{rest}V_{la}(t)$ ml, rest volume of left atrium
 $\text{rest}V_{lv}(t)$ ml, rest volume of left ventricle
 $P_{la}(t)$ mm Hg, pressure in left atrium
 $P_{lv}(t)$ mm Hg, pressure in left ventricle
 $P_{ao}(t)$ mm Hg, pressure in aorta
 $P_{ar}(t)$ mm Hg, pressure in systemic arteries

Pvein(t) mm Hg, pressure in systemic veins
 Fmit(t) liters/min, flow in left atrium
 Faov(t) liters/min, flow in left ventricle
 Far(t) liters/min, flow in systemic arteries
 Fvein(t) liters/min, flow in systemic veins

Initial Conditions of State Variables (Normotensive Case), $t = 0$ s

Fao(0) = 0.30 liters/min, flow in aorta
 Vla(0) = 59.1 ml, volume of left atrium
 Vlv(0) = 125.9 ml, volume of left ventricle
 Vao(0) = 34.5 ml, volume of aorta
 Var(0) = 327.5 ml, volume of systemic arteries
 Vvein(0) = 1910.1 ml, volume of systemic veins

State Variables for Normotensive Case

Fao(t) liters/min, flow of aorta
 Vla(t) ml, volume of left atrium
 Vlv(t) ml, volume of left ventricle
 Vao(t) ml, volume of aorta
 Var(t) ml, volume of systemic arteries
 Vlv(t) ml, volume of systemic veins

Appendix B: LV Volume Calculation

A variation of the “stacked coin” methodology used clinically to determine LV volumes from echocardiographic images was utilized [25]. The endocardial nodes in the FE LV model corresponding to short axis slices were used to determine an effective radius through fitting a circle to the endocardial node points using a least squares approximation [26]. The volume between each of these layers was approximated as a truncated circular cone so that each incremental volume was determined by

$$\Delta V = \frac{\pi}{3} h (R_1^2 + R_2^2 + R_1 R_2) \quad (B1)$$

where R_1 is the radius of a layer of endocardial nodes, and R_2 is the radius of an adjacent set of endocardial nodes (next layer). h is the axis distance between the layers as determined by taking the difference between the average of the long axis coordinates for a given layer and the average of the adjacent layer. The incremental volumes were summed to determine the total LV lumen volume. However, given the modular nature of the interface program, other measures of LV volume could easily be substituted for this one.

References

- Veress, A. I., Segars, W. P., Weiss, J. A., Tsui, B. M., and Gullberg, G. T., 2006, “Normal and Pathologic NCAT Image and Phantom Data Based on Physiologically Realistic Left Ventricle Finite-Element Models,” *IEEE Trans. Med. Imaging*, **25**(12), pp. 1604–1616.
- Mazhari, R., Omens, J. H., Waldman, L. K., and McCulloch, A. D., 1998, “Regional Myocardial Perfusion and Mechanics: A Model-Based Method of Analysis,” *Ann. Biomed. Eng.*, **26**(5), pp. 743–755.
- Walker, J. C., Ratcliffe, M. B., Zhang, P., Wallace, A. W., Fata, B., Hsu, E. W., Saloner, D., and Guccione, J. M., 2005, “MRI-Based Finite-Element Analysis of Left Ventricular Aneurysm,” *Am. J. Physiol. Heart Circ. Physiol.*, **289**(2), pp. H692–700.
- Walker, J. C., Guccione, J. M., Jiang, Y., Zhang, P., Wallace, A. W., Hsu, E. W., and Ratcliffe, M. B., 2005, “Helical Myofiber Orientation After Myocardial Infarction and Left Ventricular Surgical Restoration in Sheep,” *J. Thorac. Cardiovasc. Surg.*, **129**(2), pp. 382–390.
- Veress, A., Segars, W., Tsui, B., and Gullberg, G., 2011, “Incorporation of a Left Ventricle Finite Element Model Defining Infarction Into the XCAT Imaging Phantom,” *IEEE Trans. Med. Imaging*, **30**(4), pp. 915–927.
- Walker, J. C., Ratcliffe, M. B., Zhang, P., Wallace, A. W., Hsu, E. W., Saloner, D. A., and Guccione, J. M., 2008, “Magnetic Resonance Imaging-Based Finite Element Stress Analysis After Linear Repair of Left Ventricular Aneurysm,” *J. Thorac. Cardiovasc. Surg.*, **135**(5), pp. 1094–1102.
- Zhang, P., Guccione, J. M., Nicholas, S. I., Walker, J. C., Crawford, P. C., Shamal, A., Acevedo-Bolton, G., Guttman, M. A., Ozturk, C., McVeigh, E. R., Saloner, D. A., Wallace, A. W., and Ratcliffe, M. B., 2007, “Endoventricular Patch Plasty for Dyskinetic Anteroapical Left Ventricular Aneurysm Increases Systolic Circumferential Shortening in Sheep,” *J. Thorac. Cardiovasc. Surg.*, **134**(4), pp. 1017–1024.
- Wall, S. T., Walker, J. C., Healy, K. E., Ratcliffe, M. B., and Guccione, J. M., 2006, “Theoretical Impact of the Injection of Material Into the Myocardium: A Finite Element Model Simulation,” *Circulation*, **114**(24), pp. 2627–2635.
- Guccione, J. M., Walker, J. C., Beitel, J. R., Moonly, S. M., Zhang, P., Guttman, M. A., Ozturk, C., McVeigh, E. R., Wallace, A. W., Saloner, D. A., and Ratcliffe, M. B., 2006, “The Effect of Anteroapical Aneurysm Plication on End-Systolic Three-Dimensional Strain in the Sheep: A Magnetic Resonance Imaging Tagging Study,” *J. Thorac. Cardiovasc. Surg.*, **131**(3), pp. 579–586.
- Kerckhoffs, R. C., Neal, M. L., Gu, Q., Bassingthwaite, J. B., Omens, J. H., and McCulloch, A. D., 2007, “Coupling of a 3D Finite Element Model of Cardiac Ventricular Mechanics to Lumped Systems Models of the Systemic and Pulmonic Circulation,” *Ann. Biomed. Eng.*, **35**(1), pp. 1–18.
- Kerckhoffs, R. C., Lumens, J., Vernooij, K., Omens, J. H., Mulligan, L. J., Delhaas, T., Arts, T., McCulloch, A. D., and Prinzen, F. W., 2008, “Cardiac Resynchronization: Insight From Experimental and Computational Models,” *Prog. Biophys. Mol. Biol.*, **97**(2–3), pp. 543–561.
- Kerckhoffs, R. C., McCulloch, A. D., Omens, J. H., and Mulligan, L. J., 2009, “Effects of Biventricular Pacing and Scar Size in a Computational Model of the Failing Heart With Left Bundle Branch Block,” *Med. Image Anal.*, **12**(2), pp. 362–369.
- Bassingthwaite, J. B., Beard, D. A., Carlson, B. E., Dash, R. K., and Vinnakota, K., 2012, “Modeling to Link Regional Myocardial Work, Metabolism and Blood Flows,” *Ann. Biomed. Eng.*, **40**, pp. 2379–2398.
- Maker, B. N., Ferencz, R. M., and Hallquist, J. O., 1990, “NIKE3D: A Nonlinear, Implicit, Three-Dimensional Finite Element Code for Solid and Structural Mechanics,” Lawrence Livermore National Laboratory, Technical Report No. UCRL-MA-105268.
- Neal, M. L., and Bassingthwaite, J. B., 2007, “Subject-Specific Model Estimation of Cardiac Output and Blood Volume During Hemorrhage,” *Cardiovasc. Eng.*, **7**(3), pp. 97–120.
- Physiome Project, 2012, “Models # 153 and #154,” www.physiome.org
- Weiss, J. A., Maker, B. N., and Govindjee, S., 1996, “Finite Element Implementation of Incompressible, Transversely Isotropic Hyperelasticity,” *Comput. Methods Appl. Mech. Eng.*, **135**, pp. 107–128.
- Guccione, J. M., and McCulloch, A. D., 1993, “Mechanics of Active Contraction in Cardiac Muscle: Part I-Constitutive Relations for Fiber Stress That Describe Deactivation,” *J. Biomech. Eng.*, **115**, pp. 72–81.
- Guccione, J. M., and McCulloch, A. D., 1993, “Mechanics of Active Contraction in Cardiac Muscle: Part II-Constitutive Relations for Fiber Stress That Describe Deactivation,” *J. Biomech. Eng.*, **115**, pp. 82–90.
- Berne, R. M., and Levy, M. N., 1998, Physiology, Mosby, St. Louis, MO.
- Chan, I. S., Goldstein, A. A., and Bassingthwaite, J. B., 1993, “SENSOP: A Derivative-Free Solver for Non-Linear Least Squares With Sensitivity Scaling,” *Ann. Biomed. Eng.*, **21**, pp. 621–631.
- Physiome Project, 2012, “Sensop,” www.physiome.org/jsim/docs/Solver_Optim_Ref.html#sensop
- Papakonstantinou, J., 2007, “A Historical Development of the (n+1)-Point Secant Method,” M.A. thesis, Rice University, Houston, TX.
- Wenk, J. F., Ge, L., Zhang, Z., Soleimani, M., Potter, D. D., Wallace, A. W., Tseng, E., Ratcliffe, M. B., and Guccione, J. M., 2012, “A Coupled Biventricular Finite Element and Lumped-Parameter Circulatory System Model of Heart Failure,” *Comput. Methods Biomech. Biomed. Eng.*, 2012 Jan 16.
- Perrino, A. C., and Reeves, S., 2007, A Practical Approach to Transesophageal Echocardiography, Lippincott, New York.
- Weisstein, E. W., 2013, “Least Squares Fitting,” www.mathworld.wolfram.com/LeastSquaresFitting.html